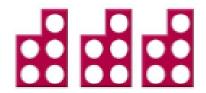


3 x 5=

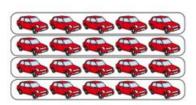




Holly Lodge Primary Academy Calculation Policy



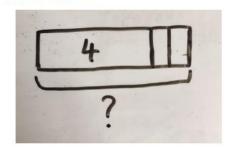
Understand the relationship between multiplication facts and division.



4 groups of 5 cars is 20 cars in total. 20 divided by 4 is 5. Calculate the difference between 8 and 5.



A bar model which encourages the children to count on, rather than count all.



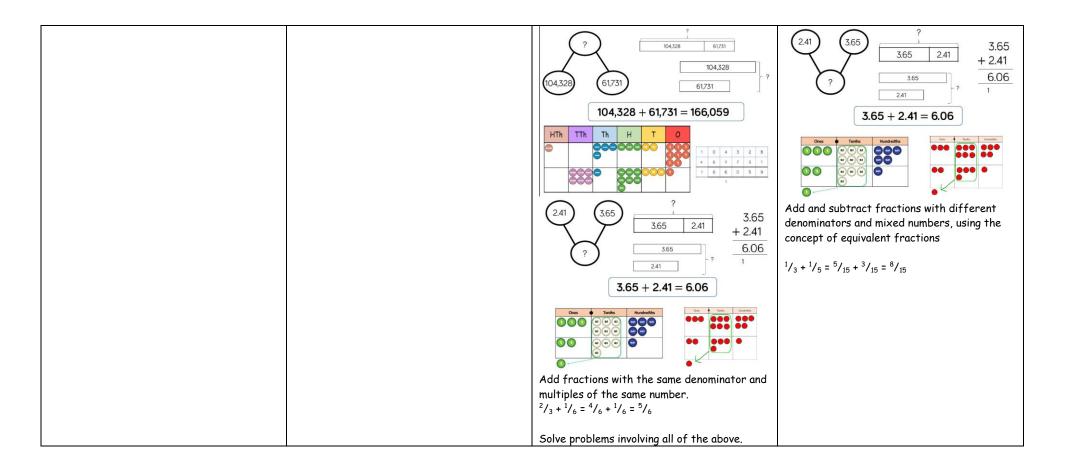
Addition

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Rec	Year 1	Year 2
-To be able to subitise (amounts to 5 then 10) -Say the number that is one more than a number from at least 1 to 5Find the total number of items in two groups by counting all of themIn practical activities and discussion, beginning to use the vocabulary involved in adding when combining two groups In practical activities and discussion, beginning to use the vocabulary involved in subtraction when subtracting from a groupCount on and back from a number other than 0.	-Read, write and interpret mathematical statements involving addition (+) and (=) signsRepresent and use number bonds within 20 -Add and one-digit and two-digit numbers to 20, including zero -Solve one-step problems that involve addition using concrete objects and pictorial representations, and missing number problems such as 4 + = 7	-Solve addition problems using concrete objects and pictorial representations, including: a two-digit number and ones a two-digit number and tens two two-digit numbers adding three one-digit numbers -Recall and use addition facts to 20 fluently, and derive and use related facts up to 100 -Show that addition of two numbers can be done in any order (commutative) -Use the inverse relationship between addition and subtraction to check calculations and solve missing number problems. -Start to record addition in columns.
Add, more, make, sum, total, altogether, one more, two more, ten more, how many more to make?, how many more isthan? Subtract, fewer,less,1 less, 2 less, How many are left? Oral and practical work Songs and rhymes Dice and number games Use Part Part whole model Number stories for combining sets eg 3 pigs in a field, 2 in a sty how many altogether? Teacher models 3+2=5 using a range of objects Number track 1 2 3 4 3 6 7 8 9 10 31 12 13 14 13 16 17 18 19 20 Number bonds for numbers up to 10 Full number lines	Songs and rhymes Working with apparatus such as bead strings to 20, cubes, dienes, Numicon: Use + and = signs and associated vocabulary. Adding more than 2 numbers Putting the larger number first 13+3= 13 in your head or on fingers Counting in 10s from multiples of 10 Number bonds of all numbers to 20 \[+7 = 12 9 + = 18 \]	Counting in 10s from any number Rapid recall of all number bonds for all numbers to 20. Use of numicon, dienes, bar model, part whole model to demonstrate. $7 + 6 + 3 = 16$ $7 + 6 + 3 = 16$

Structured number lines and bead strings to 100
Use of tens frames
8+7=15 2 5
Commutative law
12 + 11 = 33 11 + 12 = 33
Start to record addition in columns 71 13 + 84 Can check by using inverse operation, use to solve missing box problems
Eg + 5= 23 Stem sentences used.

Addition

Year 3	Year 4	Year 5	Year 6
-Add a range of numbers mentally, including: a three-digit number and ones a three-digit number and tens a three-digit number and hundreds -Add numbers with up to three digits, using formal written methods of columnar addition -Estimate the answer to a calculation and use inverse operations to check answers -Solve problems, including missing number problems, using number facts, place value, and more complex addition. -Add fractions with the same denominator within one whole (for example, ⁵ / ₇ + ¹ / ₇ = ⁶ / ₇)	-Add numbers with up to 4 digits using the formal written methods of columnar addition where appropriate -Estimate and use inverse operations to check answers to a calculation -Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and whyAdd fractions with the same denominator -Solve simple measure and money problems involving fractions and decimals to two decimal places	-Add whole numbers with more than 4 digits, including using formal written methods (columnar addition) -Add numbers mentally with increasingly large numbers (e.g. 8 462 + 2300 = 10 762)Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy -Solve addition and subtraction multi-step problems in contexts, including to 3 decimal places, deciding which operations and methods to use and whyAdd and subtract fractions with the same denominator and denominators that are multiples of the same number	-Add whole numbers with more than 4 digits, including using formal written methods (columnar addition) -Perform mental calculations, including with mixed operations and large numbers -Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why -Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
Use partitioning to support mental calculations. Using an empty number line to count on. 274 + 132 Add a near multiple of 10 to a two-digit number Continue as in Year 2 but with appropriate numbers e.g. 350 + 189 is the same as 350 + 190 - 1. Extend use of columnar addition, developing more compact recording to tackle larger numbers.	Use formal column addition for numbers with 4 digits 1271 2243 + 3514 1 Extend to decimals, using an empty number line. (pic)	Use formal column addition for numbers with more than 4 digits. 21271 12243 + 33514 1 Including method were carrying is used. Extend to decimals. 42.432 12.713 + 55.145 1 Develop reasoning skills by using a range of representations including part whole models, number sentences, place value counter problems and bar models.	Use formal column addition for any numbers which cannot be added mentally (>1 million) 2353248 $1254173 + \\ 3607421$ $1 $



Subtraction

	Subtraction	
Rec	Year 1	Year 2
-Say the number that is one less than a number from 1 to 20In practical activities and discussion, beginning to use the vocabulary involved in subtraction when taking away objects groups.	-Read, write and interpret mathematical statements involving addition (-) and (=) signsRepresent and use number bonds and related subtraction facts within 20 -Subtract one-digit and two-digit numbers to 20, including zero -Solve one-step problems that involve subtraction using concrete objects and pictorial representations, and missing number problems such as 8 - □= 5	-Solve subtraction problems using concrete objects and pictorial representations, including: a two-digit number and ones a two-digit number and tens two two-digit numbers -Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 -Show that subtraction of one number from another cannot be done in any orderUse the inverse relationship between addition and subtraction to check calculations and solve missing number problemsStart to record subtraction in columns.
Take (away), leave, how many are left/left over? How many have gone? One less, two less, ten less, is the same as Oral and practical work Songs and rhymes	Songs and rhymes Working with apparatus Bead strings to 20. Cubes, dienes, bar model.	Counting back in 10s from any number to 100 Jumping back on a structured number line. 76-34 +2 +30 +5
Dice and number games, counting back, taking away. Use of number tracks. 1 2 3 4 5 6 7 8 9 Number stories using objects	Subtraction with Numicon. 9 - 3 = 6	28 30 60 65
8-3= A A A A A A A A A A A A A A A A A A A	Physical and practical work on structured number lines eg jumping backwards Number stories, 15 people on a bus 3 get off, how many are left on? Putting a number in your head and counting back with fingers to help.	Finding the difference between 2 towers of cubes leading to using the structured number line or fingers for numbers that are close together to calculate difference by counting on eg
How many are there? How many now? (after some have been removed) Teacher modelling number sentences, 8 take away 3 is 5	12 - 3 = 15 - = 4 - 11 = 4 Counting back in 10s from multiples of 10s Giving change to 20p Finding the difference by counting on, comparing quantities	42 - 39 = 3 Use addition as the inverse operation to check and in empty box problems e.g. - 8=12

Fact families to help with the understanding of commutativity
in addition but not in subtraction
6 + 4 = 10
4 + 6 = 10
10 - 6 = 4
10 - 4 = 6
Stem sentences used.

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	Odbii	action	
Year 3	Year 4	Year 5	Year 6
-Subtract a range of numbers mentally, including: a three-digit number and ones three-digit number and tens a three-digit number and hundreds -Subtract numbers with up to three digits, using formal written methods of columnar subtraction -Estimate the answer to a calculation and use inverse operations to check answers -Solve problems, including missing number problems, using number facts, place value, and more complex additionSubtract fractions with the same denominator within one whole (for example,	-Subtract numbers with up to 4 digits using the formal written methods of columnar subtraction where appropriate -Estimate and use inverse operations to check answers to a calculation -Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and whySubtract fractions with the same denominator -Solve simple measure and money problems involving fractions and decimals to two decimal places	-Subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction) -Subtract numbers mentally with increasingly large numbers (e.g. 10 462 - 2300 = 8 162)Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy -Solve addition and subtraction multi-step problems in contexts, including to 3 decimal places, deciding which operations and methods to use and whyAdd and subtract fractions with the same denominator and denominators that are multiples of the same number	-Subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction) -Perform mental calculations, including with mixed operations and large numbers -Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why -Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions

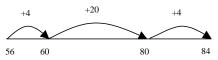
Develop confidence in counting back in 100s, 10s and 1s from any number.

Use an empty number line to count back. 297-126=



Count on to find the difference using empty number line

84-56=



Expanded method of decomposition and beginning to record in a more compact method for numbers too large to do mentally.

4 9 8

Using dienes and column subtraction to find the difference between two numbers. (Up to 4 digits)

Extend to decimals to 2 decimal places.

Expanded method of decomposition, leading to more compact recording.

Extend to decimals.

Formal method used for both calculations with and without borrowing

874 - 523 becomes

Answer: 351

932 – 457 becomes

Answer: 475

Move towards compact decomposition, including decimals.

Subtract fractions with the same denominator and multiples of the same number.

$$\frac{2}{3} - \frac{1}{6} = \frac{4}{6} - \frac{1}{6} = \frac{3}{6}$$

Use formal method of compact decomposition. 21

Apply to problem solving contexts e.g. money and measures

Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions

$$^{1}/_{3}$$
 - $^{1}/_{5}$ = $^{5}/_{15}$ - $^{3}/_{15}$ = $^{2}/_{15}$
Revert to expanded methods if the children experience any difficulty.

Multiplication

Rec	Year 1	Year 2
-Start to solve problems involving doubling.	-Solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. -Make connections between arrays, number patterns, and counting in twos, fives and tens.	-Recall and use multiplication facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers -Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (*) and equals (=) signs -Show that multiplication of two numbers can be done in any order (commutative) -Solve problems involving multiplication using materials, arrays, repeated addition, mental methods and multiplication and including problems in contexts.
Counting in ones, twos, tens	Counting in twos, fives and tens (using fingers to help count in	Counting in 3s
Odd and even numbers	multiples)	Doubles of all numbers up to 10 and doubles of multiples of 10
Matching pairs e.g.	Knowing doubles of numbers to 10	to 100
socks Noah's Ark	Dice and domino games with doubles	Recognise odd and even numbers, supported by Tens frames.
	Finding patterns of numbers using a 100 square and make connections with arrays. 1 2 3 4 5 6 7 8 9 10	
Songs and rhymes	81 82 83 84 85 86 87 88 89 90 911 92 93 94 95 96 97 98 99 100	Arrays and repeated addition this links to commutative law below. Use visual and concrete methods below as long with
Finding doubles in dominoes		fingers for counting. Additional language introduced including
	Repeated addition of sets of objects,	"lots of" for problem solving.
	teacher modelling 2+2+2 = 6	• • • 4 x 2 or 4 + 4
	Use coins for repeated addition	• • • •
Doubles in practical contexts.		2 x 4 or 2 + 2 + 2 + 2
Groups of objects with the same number, counting how many in		
each group, and finding how many altogether	and model using Numicon.	
		Computative law
		Commutative law $4 \times 3 = 12$
	5 5 5 45	3 x 4 = 12
	5 + 5 + 5 = 15	5 N 1 22
	Stem sentences are introduced.	Stem sentences used

Stem sentences used.

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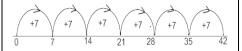
	Multi	plication	
Year 3	Year 4	Year 5	Year 6
-Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables -Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods of short multiplication -Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.	-Recall multiplication and division facts for multiplication tables up to 12 × 12 -Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1 and multiplying together three numbers -Recognise and use factor pairs and commutativity in mental calculations -Multiply two-digit and three-digit numbers by a one-digit number using formal written layout -Solve problems involving multiplying including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n	-Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers -Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers -Multiply numbers mentally drawing upon known facts, including multiplying whole numbers and those involving decimals by 10, 100 and 1000 -Recognise and use square numbers and cube numbers, write the notation for both [(²) and (³)] and solve problems involving multiplication using knowledge of factors and multiples, squares and cubes -Solve problems involving scaling by simple fractions. -Multiply proper fractions and mixed numbers by	-Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication -Multiply one-digit numbers with up to two decimal places by whole numbers -Perform mental calculations, including with mixed operations and large numbers -Multiply simple pairs of proper fractions -Identify common factors, common multiples and prime numbers
	objects are connected to m objects.	whole numbers, supported by materials and diagrams	

$$15 \times 2 = 30$$

Know that division is inverse of multiplication and multiplication is inverse of division

Understand multiplication as repeated addition

Use a number line to solve 6x7



Continue to use arrays

Grid method with resources (dienes, PVC)
Grid method with numbers

 $34 \times 5 =$

×	30	4
5	150	20

150 + 20 = 170

Long multiplication

 24×6 becomes

2 4 × 6 1 4 4 Progress towards formal short multiplication Multiplication by using known facts.

E.g. to multiply by 60, multiply by 6 then by 10

Doubling all numbers to 50, multiples of 10 to 500

Multiply decimals and integers by 10, 100 and 1000.

Revisit long multiplication for 3-digit \times 1-digit

Formal short multiplication 342 × 7 becomes

Missing number type problems e.g. $12 \times ? = 9 \times 8$,

Use methods within problem solving contexts such as money and measures. Eg apply scaling to problems such as recipes and ingredients.



Scaling problems e.g. $56 \times 4 = 50 \times ? + 6 \times ?$ Use short multiplication when multiplying by 1 digit.

	3	4
× 	3	9
	2	1

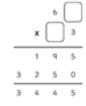
Answer: 2394

Use formal long multiplication for up to 4 digit × 2 digit

Answer: 3224

Multiply fractions by whole numbers e.g. $\frac{1}{2} \times 7$

Missing number problems



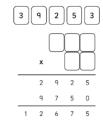
Use formal long multiplication for up to 4 digits \times 2 digits. E.g. 1354×24

Extend to decimals.

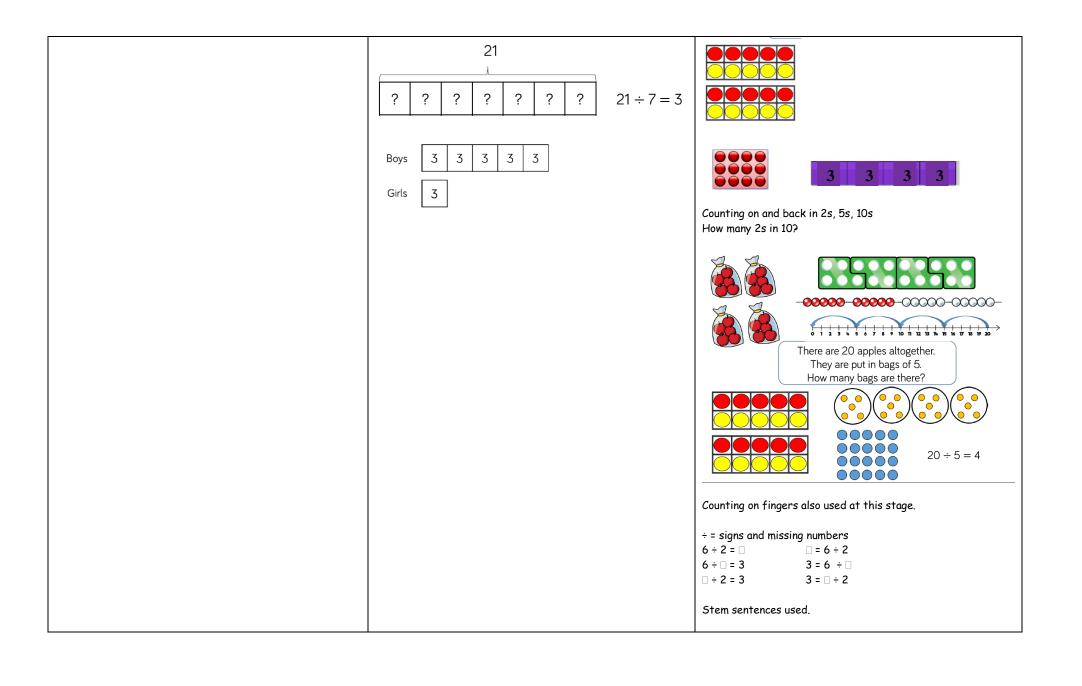
Multiply simple pairs of proper fractions.

$$\frac{2}{3} \times \frac{2}{5} = \frac{4}{15}$$

Missing number problems E.g. using the given digit cards once, complete the calculation



Division						
Rec	Year 1	Year 2				
-Start to solve problems involving halving and sharing	-Solve one-step problems involving division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.	-Recall and use division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers -Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs -Show that division of one number by another cannot be done in any order -Solve problems involving division, using materials, arrays, repeated subtraction, mental methods, and multiplication and division facts, including problems in contexts.				
Practical activities, songs and rhymes. 10 fat sausages. Sharing during snack time by giving 1 each Is there an easier way of sharing a larger amount? E.g. 2 at a time Give each friend the some number of cookies. Ladi Hulling And Welning Making groups/piles of 2, finding partners E.g. in PE grouping in 2s, how many pairs are there? 1 ball for each pair, how many balls do I need to get out?	Practical activities, songs, and games. Sharing - 6 sweets are shared between 2 people. How many do they have each? Grouping - There are 6 sweets. How many people can have 2 each? (How many 2s make 6?) Cutting cakes/ pizza in half, sharing related to fractions Finding half of a group of objects Knowing halves of even numbers to 20 Use Numicon and bar model as a representation	Relate division to fractions $\frac{1}{2}$ or $\frac{1}{4}$ of 12, 20. Half of 12 is 12÷2= Introduction of fact families and making equal groups Understand division as sharing and grouping and link to multiplication facts $12 \div 3 = 4 \qquad 12 \div 4 = 3$ $3 \times 4 = 12 \qquad 4 \times 3 = 12$ $20 \div 5 = 4$ $48 \div 2 = 24$				
	Bar model used for representation of groups in a whole					



Division

Year 3	Year 4	Year 5	Year 6
-Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables -Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers divided by one-digit numbers, using mental and progressing to formal written methods -Solve problems, including missing number problems, involving multiplication and division -Calculate simple remainders after division	-Recall multiplication and division facts for multiplication tables up to 12 × 12 -Recognise and use factor pairs in mental calculations -Divide two-digit and three-digit numbers by a one-digit number using formal written layout -Divide a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths	-Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context -Divide whole numbers and those involving decimals by 10, 100 and 1000 -Know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers -Establish whether a number up to 100 is prime and recall prime numbers up to 19	-Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context -Identify common factors, common multiples and prime numbers -Divide proper fractions by whole numbers (for example, $^{1}/_{3} \div 2 = ^{1}/_{6}$) -Associate a fraction with division and calculate decimal fraction equivalents (for example, 0 .375) for a simple fraction (for example, $^{3}/_{8}$)
$\frac{1}{4}$ or $\frac{1}{2}$ of 24, 40 etc	Sharing and grouping	Consolidate formal short division	Formal short division for 4 digit ÷ 1 digit (remainders shown as a decimal)
Understand division as grouping and as sharing. e.g. If there are 14 sweets in a bag, how	Continue to understand division as both sharing and grouping.	432 ÷ 5 becomes 8 6 r 2	1 8 6. 2 5 9 43 31. 10
many people can have 2 each? Practically demonstrate repeated subtraction to find how many groups.	Use informal or pictorial methods relating to the child's mental methods moving onto short formal method when ready.	5 4 3 2	This method can also be used for decimals. 432 ÷ 15 becomes Introduce
Remainders 17÷5= 3r2	98 ÷ 7 becomes	Complete missing number calculations	formal long 2 8 · 8 division when 1 5 4 3 2 · 0
2 7 12 17	7 9 8	6 5 9 8 N	dividing by a $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Make clear links between x and ÷ ÷ = signs and missing numbers	Teach using PVC, with numbers, without an exchange, with an exchange, with a	Quotients can be expressed as fractions or decimal fractions	1 2 0
Divide by 10 and 100	remainder Remainders e.g. 17 ÷ 5 = 3 r 2	61 ÷ 4 = 15 ½ or 15.25	Answer: 28-8
Extend to pencil and paper procedures which reflect mental methods.			

		Division of fractions using keep, change, flip.
The number line is also an excellent way of introducing the 'chunking' approach.		2 · 2 - 2 · 0 - 24 - 24
72 ÷ 5 = 14 r 2		$\frac{3}{5} \div \frac{2}{6} = \frac{3}{5} \times \frac{8}{6} = \frac{24}{40} = 2\frac{4}{10}$
		5 8 5 2 10 10
10 x 5 1x5 1x5 1x5		
0 50 55 60 65 70 72		$\underline{3} \div 2 = \underline{3} \div \underline{2} = \underline{3} \times \underline{1} = \underline{3}$
30 33 00 03 70 12		5 5 1 5 2 10
Into a more efficient		
10 x 5 4 x 5		2 <u>3</u> ÷ <u>1</u> = <u>11</u> ÷ <u>1</u> = <u>11</u> × <u>4</u> = <u>44</u> = 11
0 50 70 72		4 4 4 4 4 1 4
		Continued
		commuea
		Y6 division cont.
		Missing number questions e.g.
		Using the digit cards given, complete the
		calculation
		1 5 8 6 4
		8 5 8
		8 5 8
		Leading to long division with missing numbers:
		2 9 2
		5 3 0
		0
		3
		3
		0
		0 0
		0 0